

Adaptive Exploration for Geological Classification

A background image showing a Mars rover on a red, rocky planet surface. A bright green laser beam is projected from the rover towards the right side of the frame. The sky is a hazy, reddish-orange color.

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Overview

- Problem Introduction
- Simulation Environment
- Problem 1 – Sampling Point Selection
 - Approach 1 - Variance Method
 - Approach 2 - Clustering Method
- Problem 2 – Planning Path To Sampling Point
 - Approach 1 - Dynamic Programming (DP)
 - Approach 2 - Multi-Heuristic A*
- Conclusion

Problem Introduction

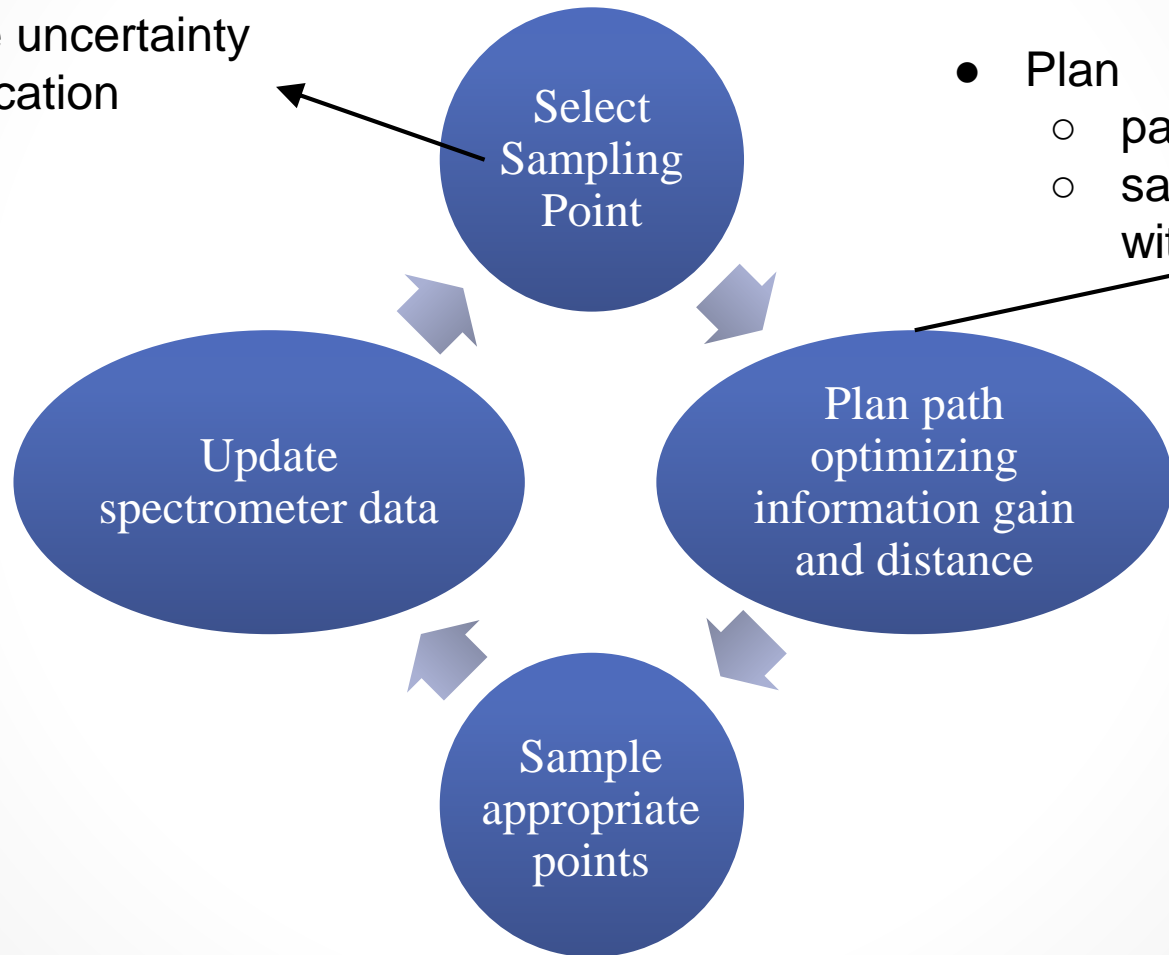
- Rover exploration of extraterrestrial bodies is slow
- One of the motives of exploration – **Rock classification**
- Spectrometer readings to classify rocks

- Satellite Spectrometers have **low wavelength and spatial resolution** and high sensor noise
- Ground based spectrometer sampling is **costly**
- Optimization Problem
- **Where to sample such that the rock classification has lowest uncertainty.**



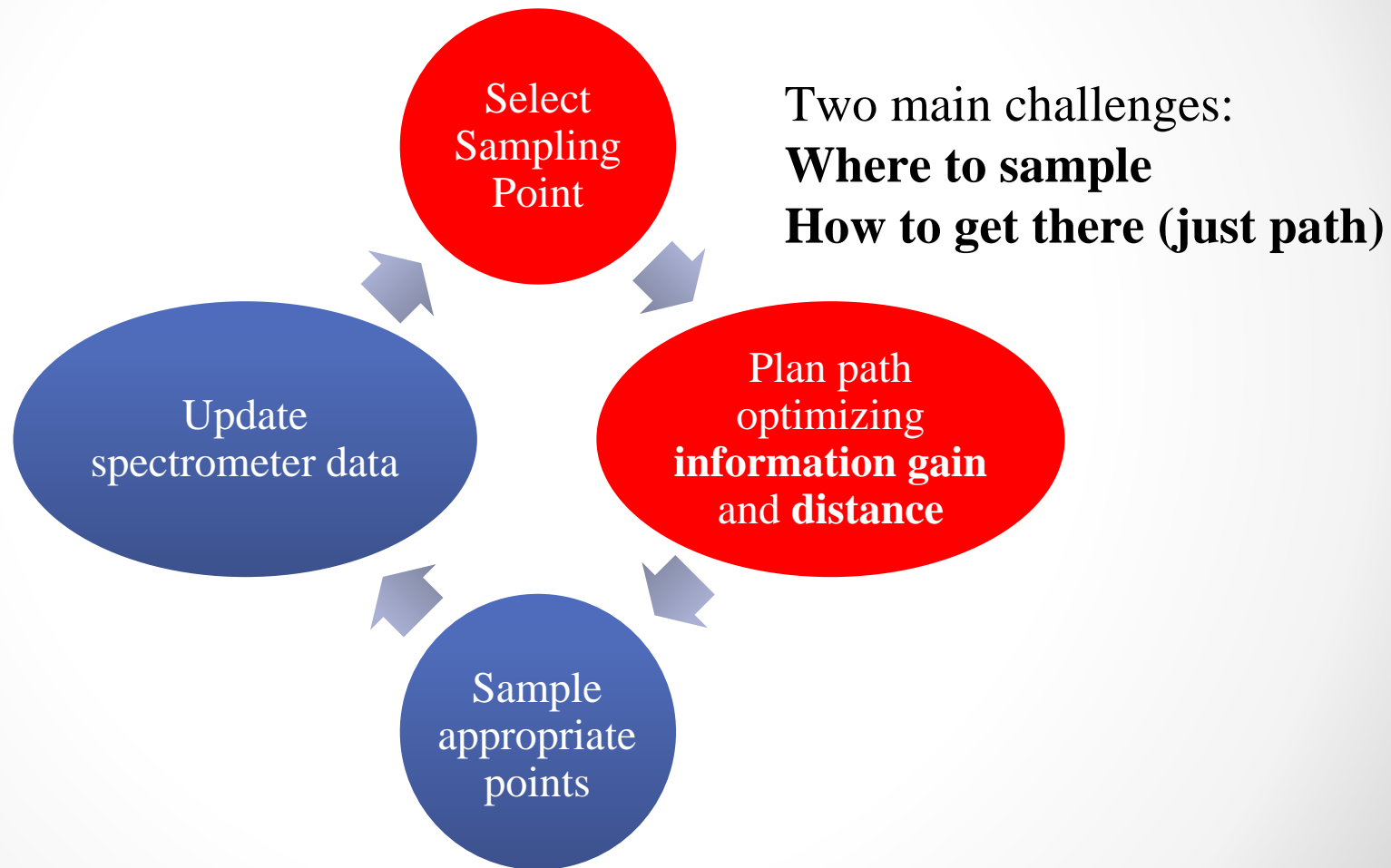
Problem Introduction

Decrease uncertainty
in classification



- Plan
 - path
 - sampling points within path

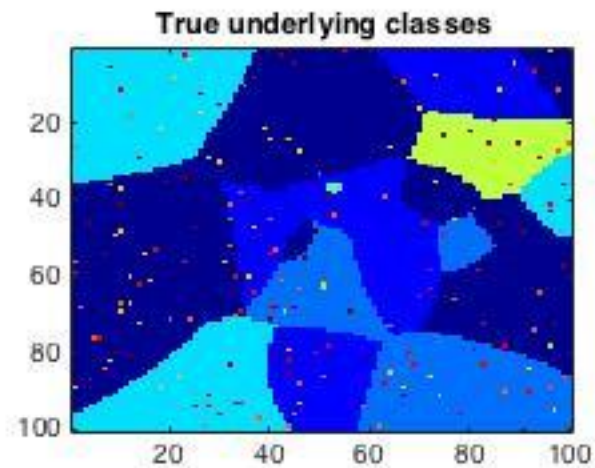
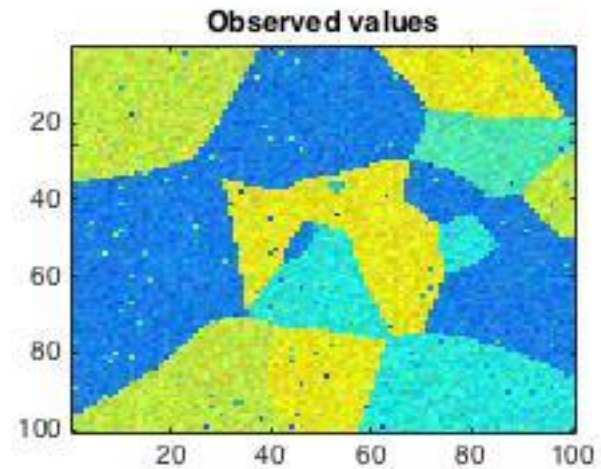
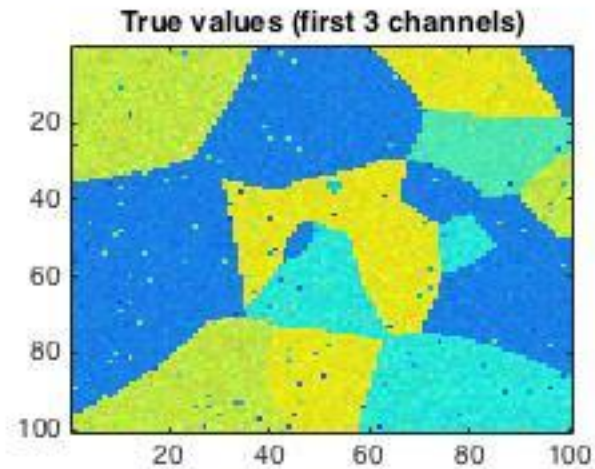
Problem Introduction



Simulation Environment

- Provides three pieces of information
- Information 1 – Satellite Reading for a region
 - Containing less number of channel
- Information 2 – Rover reading at each point in the region
 - Result of sampling a point – more number of channels (higher resolution)
- Information 3 – True classification of each point
- We control
 - Noise in sensor
 - Number of classes
 - Number of dominant and rare classes

Simulation Environment



Problem 1: Where to sample

A Mars rover is positioned on the left side of the frame, emitting a bright green laser beam that extends horizontally across the middle of the image towards the right. The background shows a vast, reddish-brown landscape with large, dark rocks in the foreground and a hazy horizon under a pale, orange sky. The overall scene is a simulated or actual view of a Mars surface.

Approach 1: Variance based Entropy

Differential Entropy-Greedy Approach

- Starting sample set: $S=\{S1\}$
- Calculate Entropy of each point in map with the sample set using

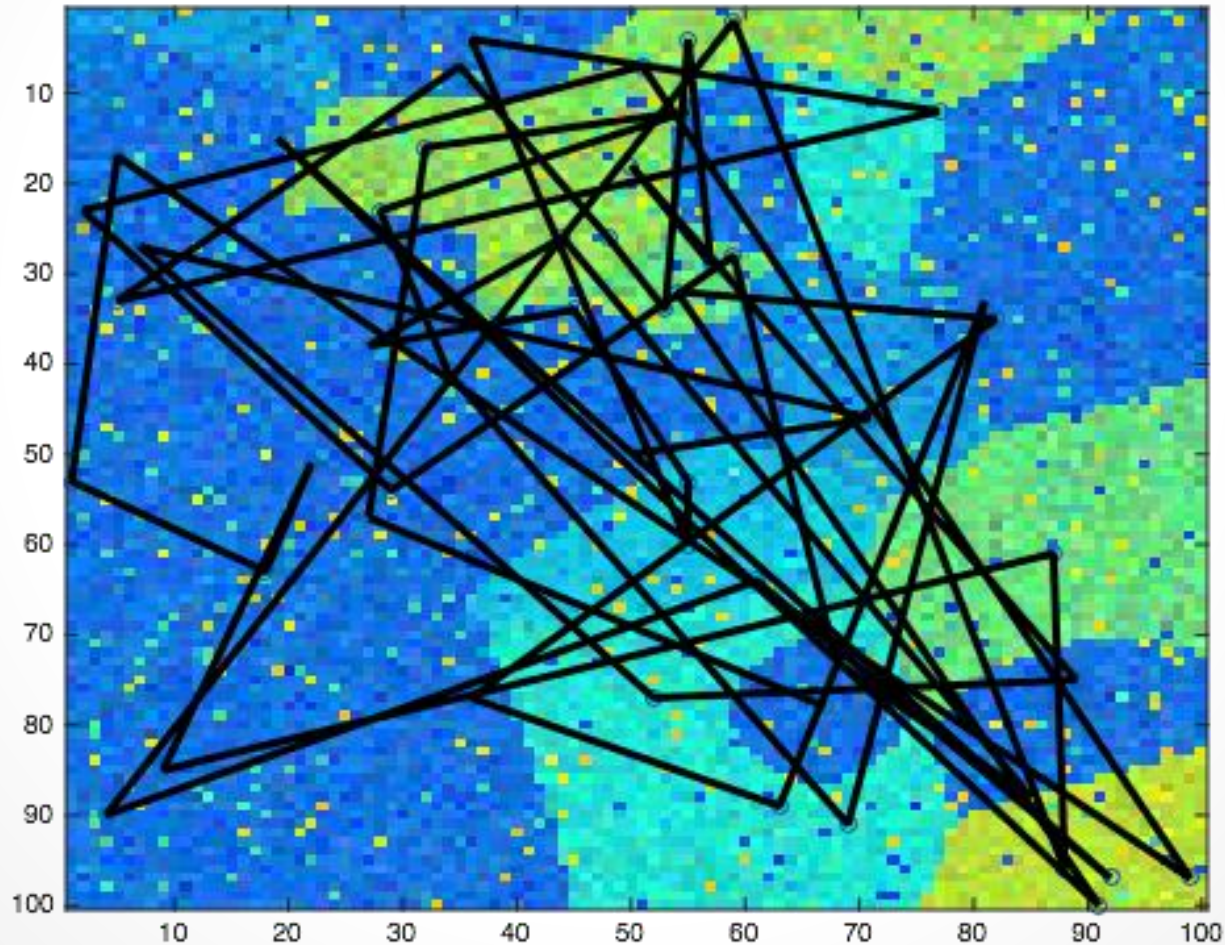
$$H(S) = \frac{1}{2} \sum_b^B \log(2\pi\sigma_b)$$

where, σ_b is the variance in the b th band of S

- Maximum Entropy point is the next sample point
- Travel to point $S2$, sample, and add it to the sample set: $S=\{S1,S2\}$
- Repeat entropy calculation
- Stop after 50 samples

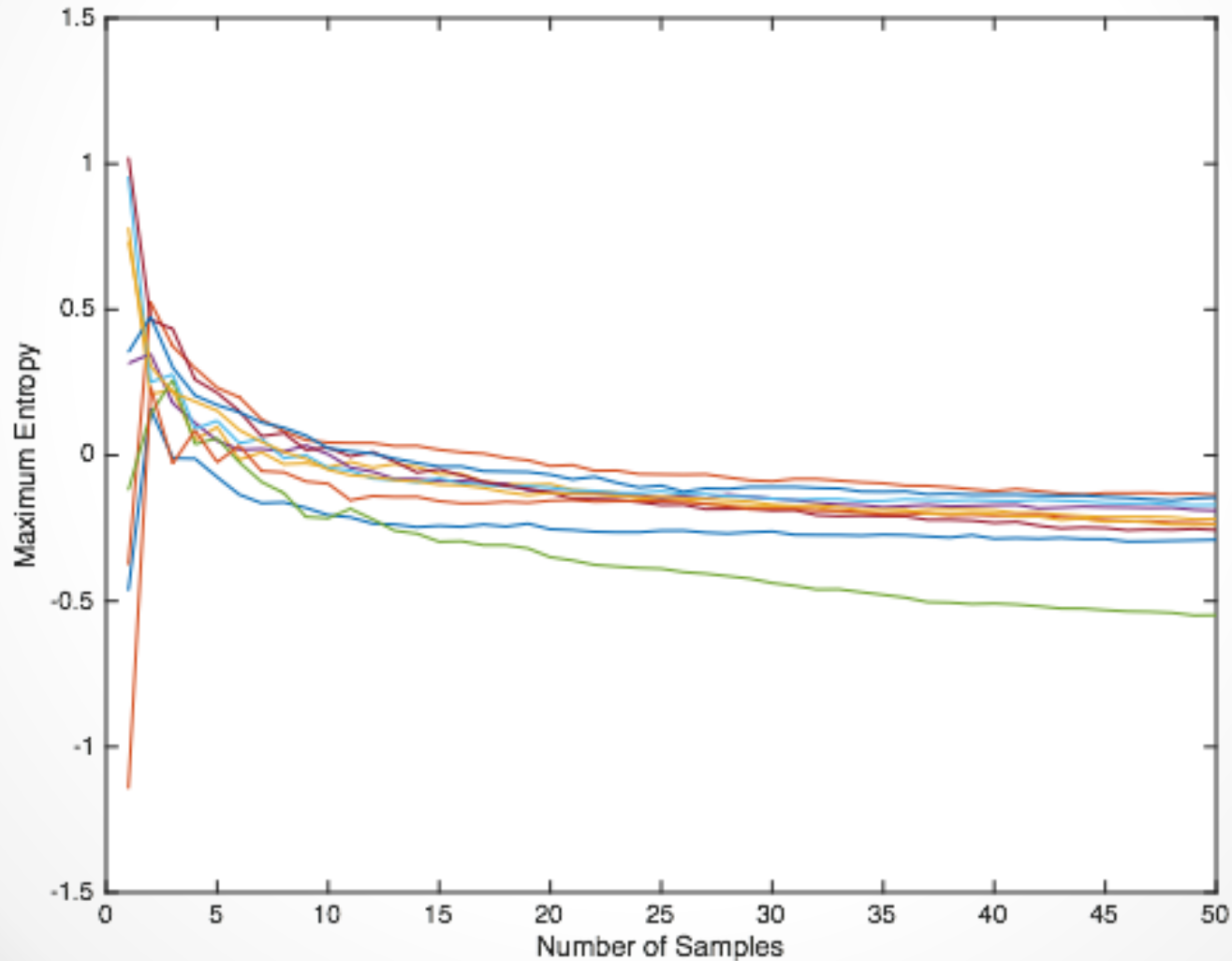
Greedy Approach - Full map

Starting point - center of map



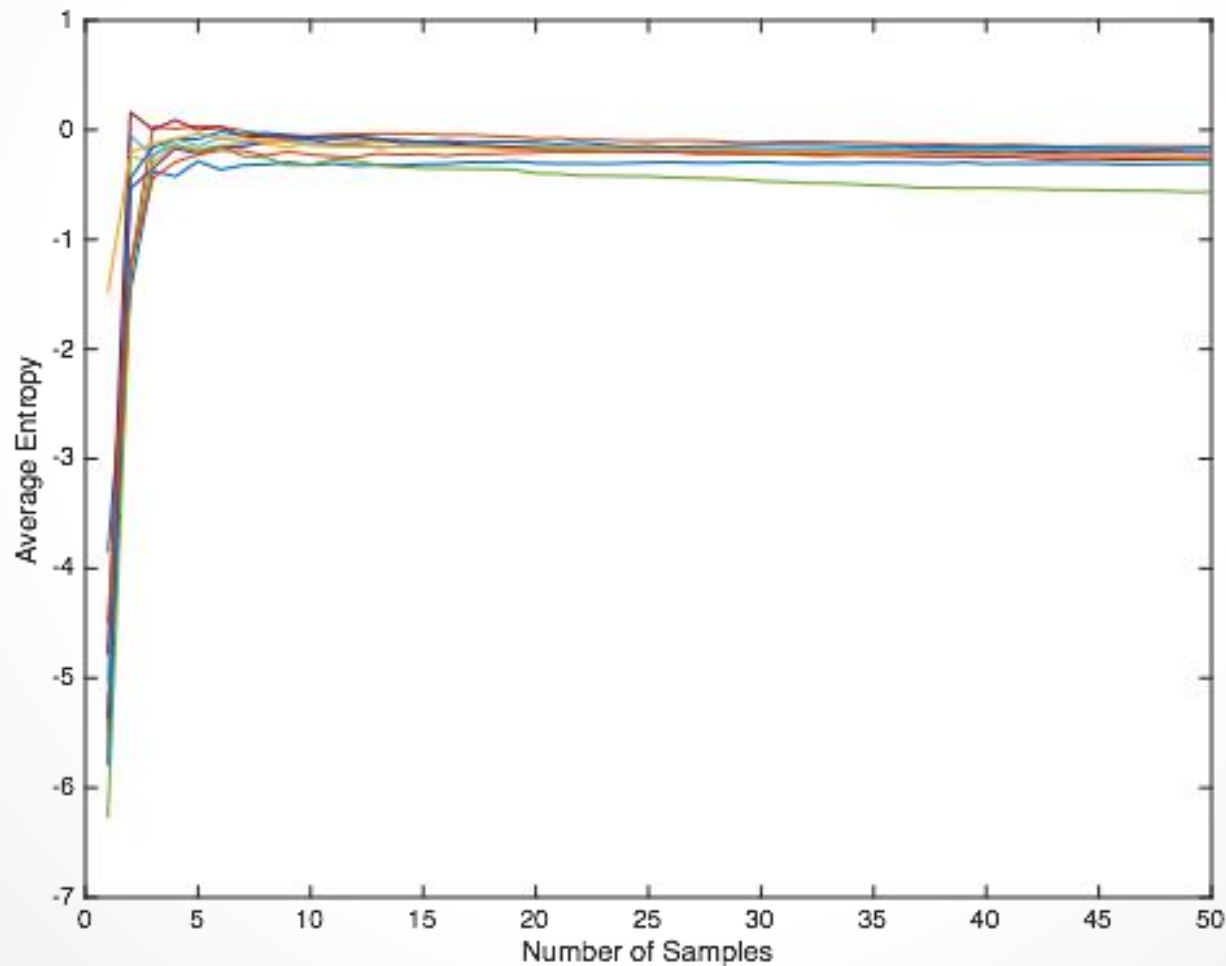
Greedy Approach - Full map

No. of Test Data = 10



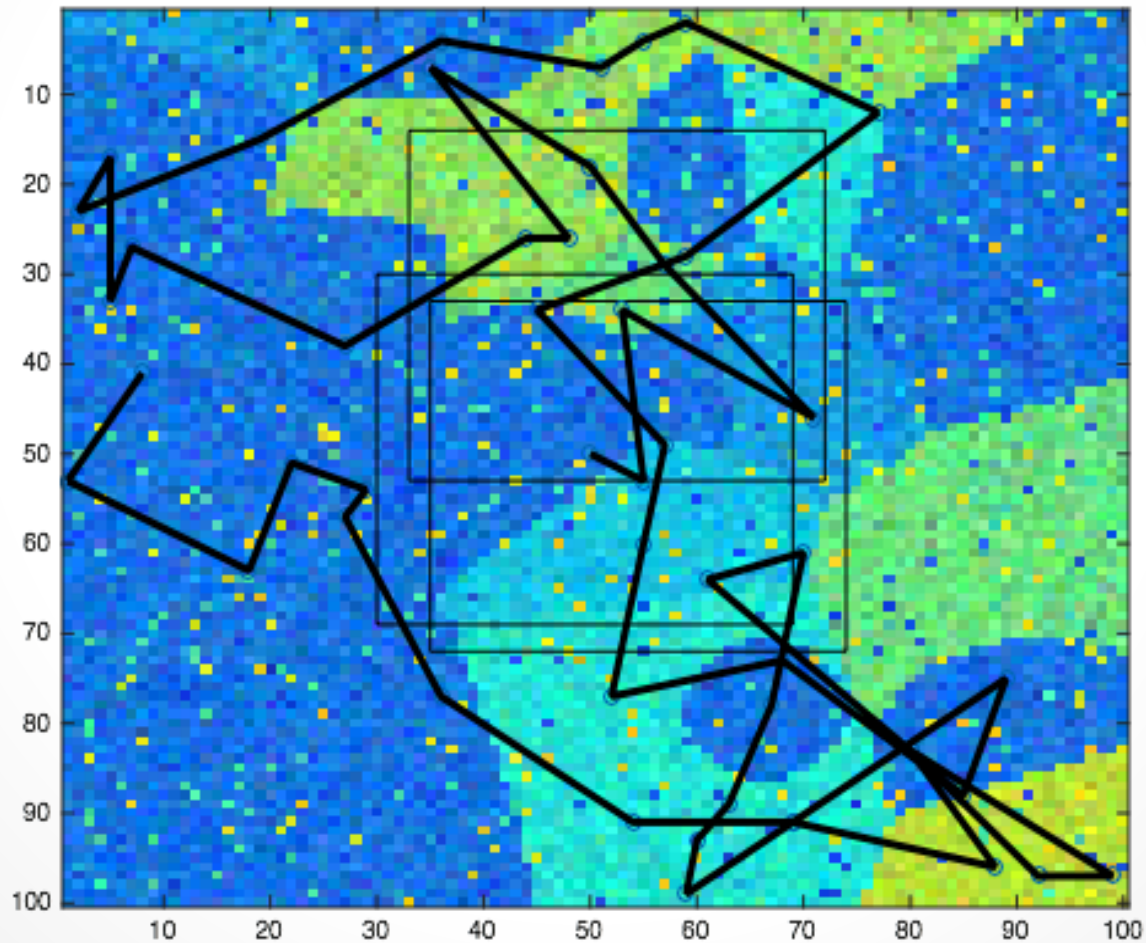
Greedy Approach - Full map

No. of Test Data = 10



Greedy Approach - window

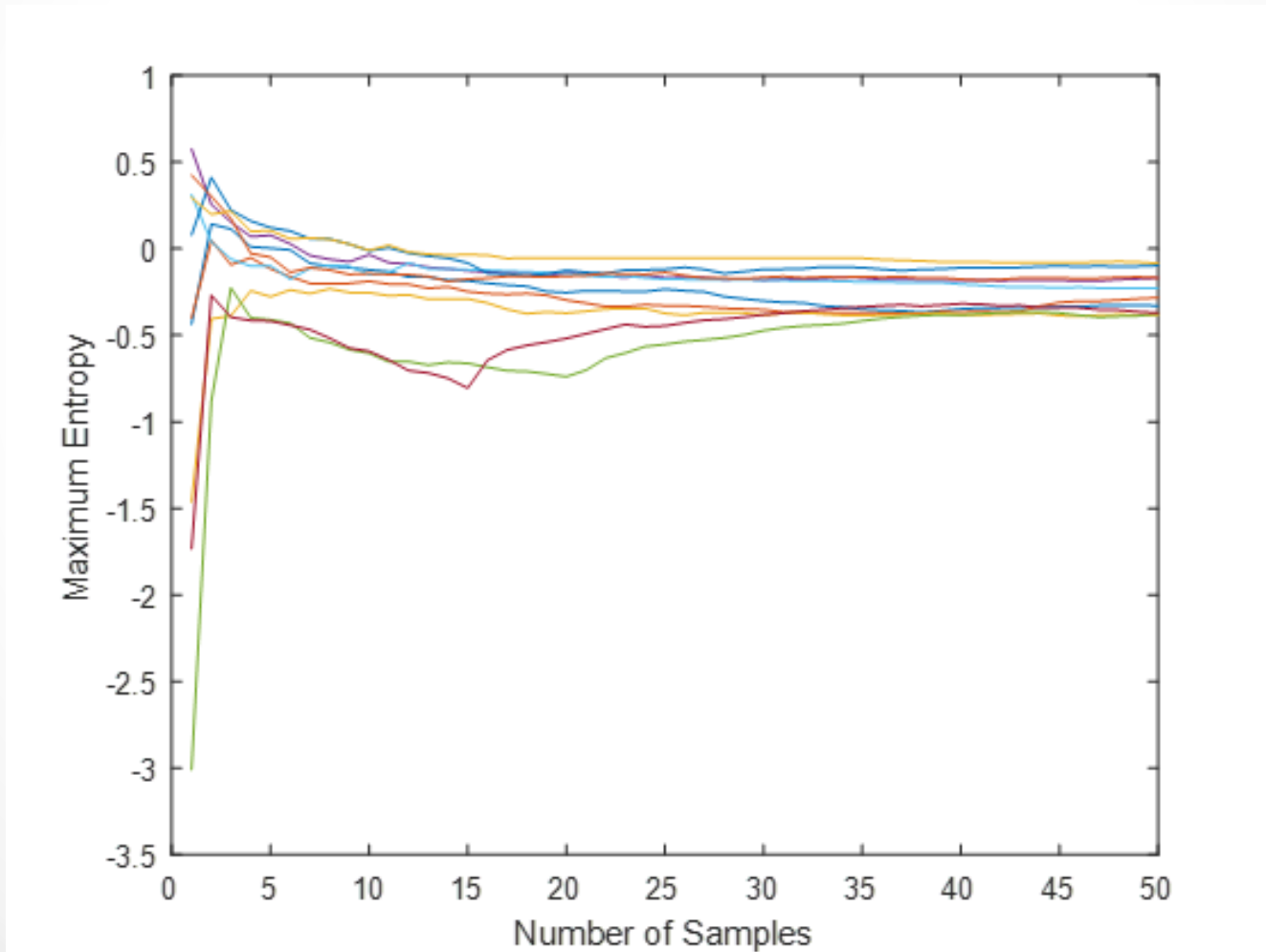
Window size ± 20



Greedy Approach - window

Window size +/-20

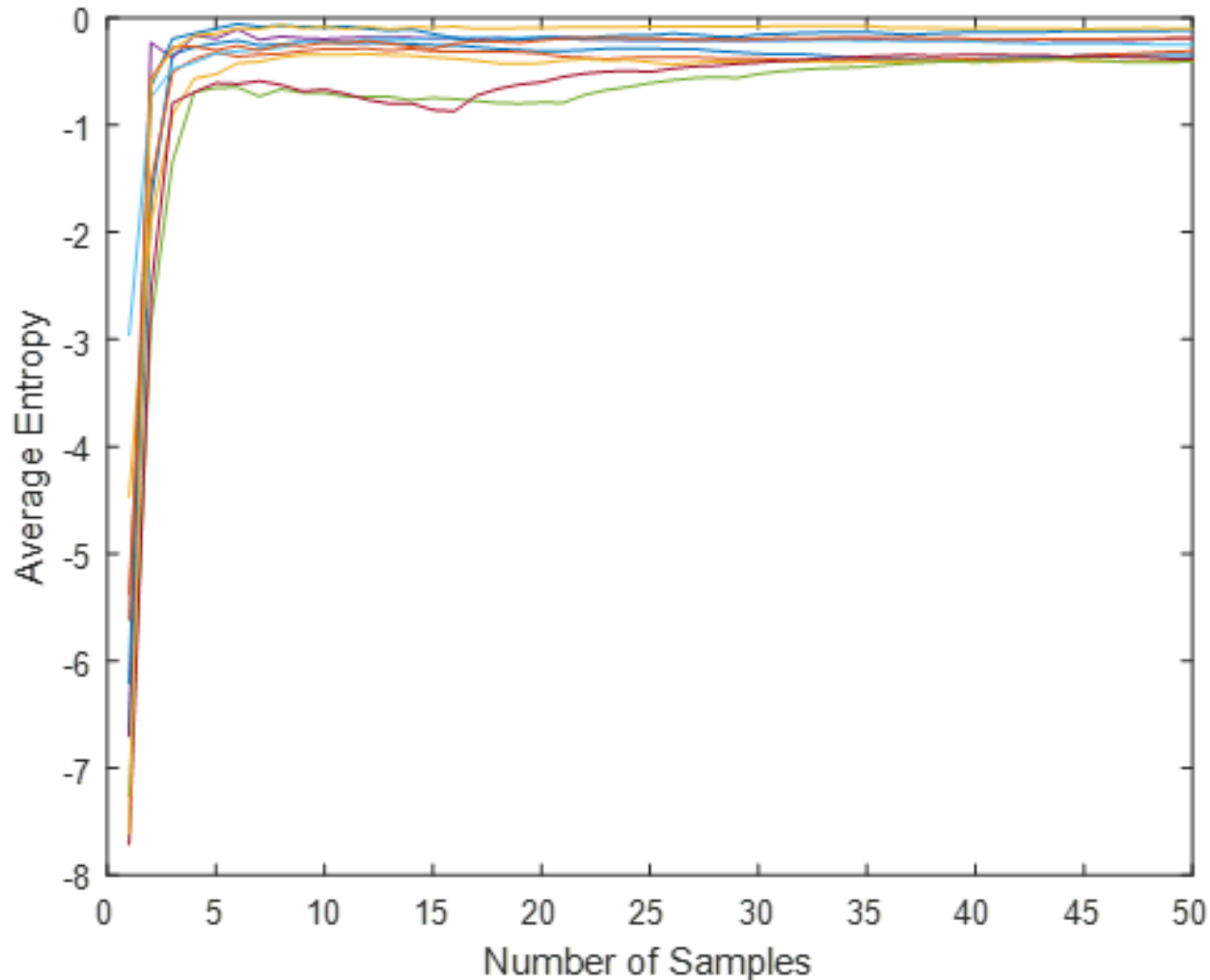
No. of Test Data = 10



Greedy Approach - window

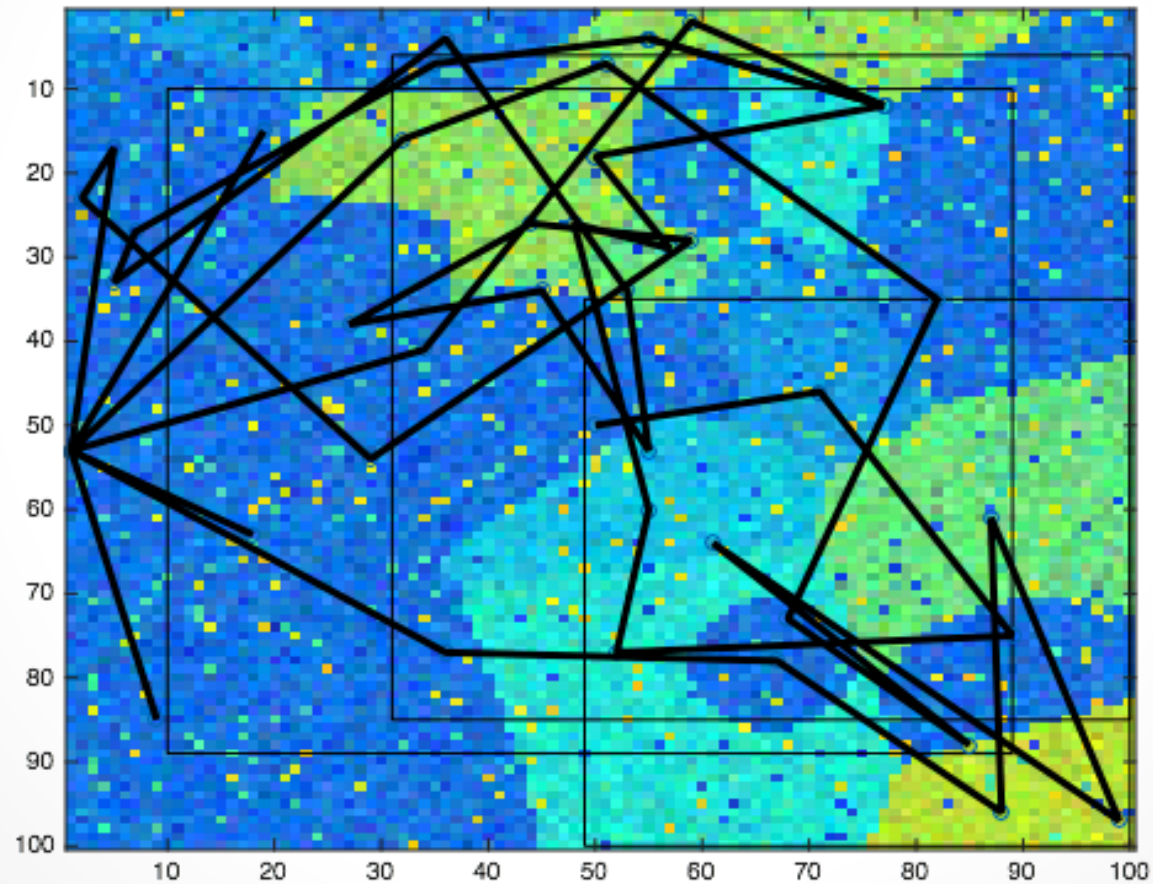
Window size ± 20

No. of Test Data = 10



Greedy Approach - window

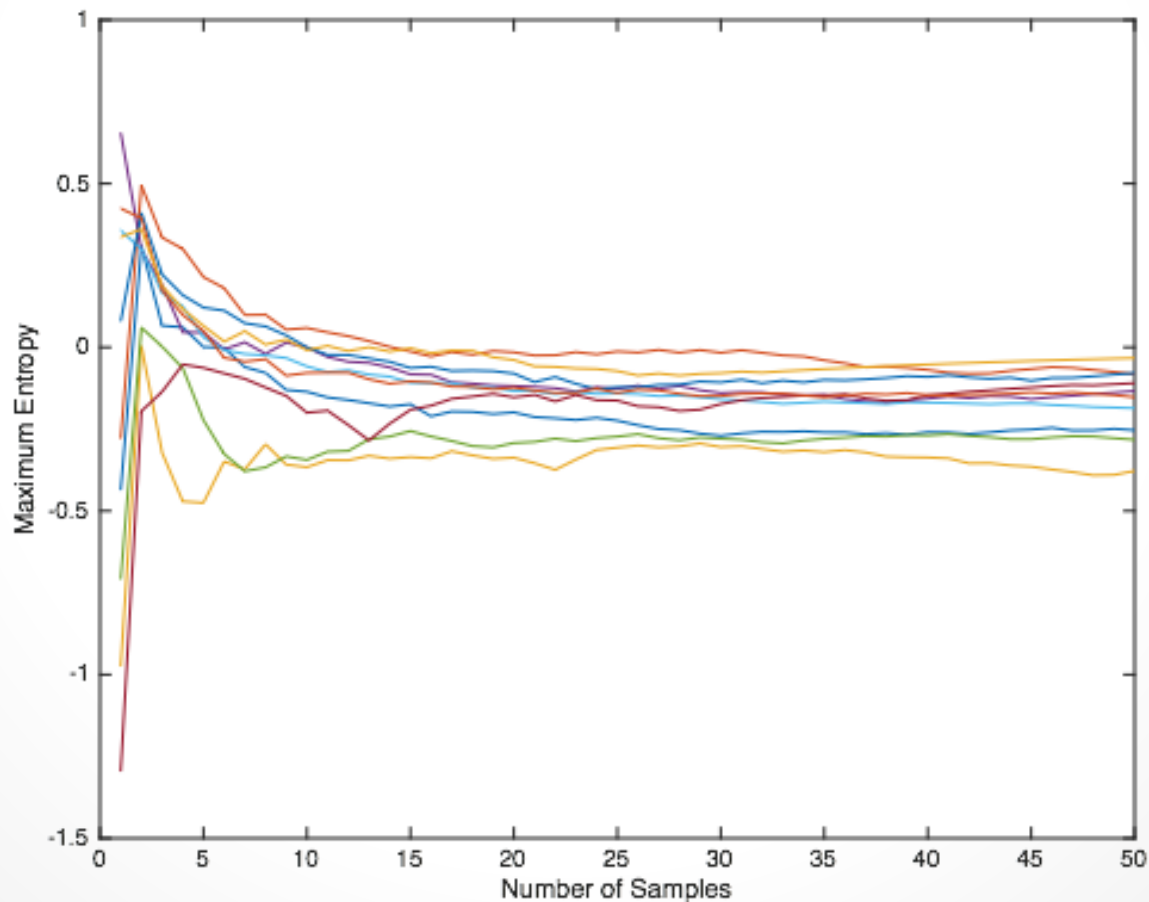
Window size ± 40



Greedy Approach - window

Window size +-40

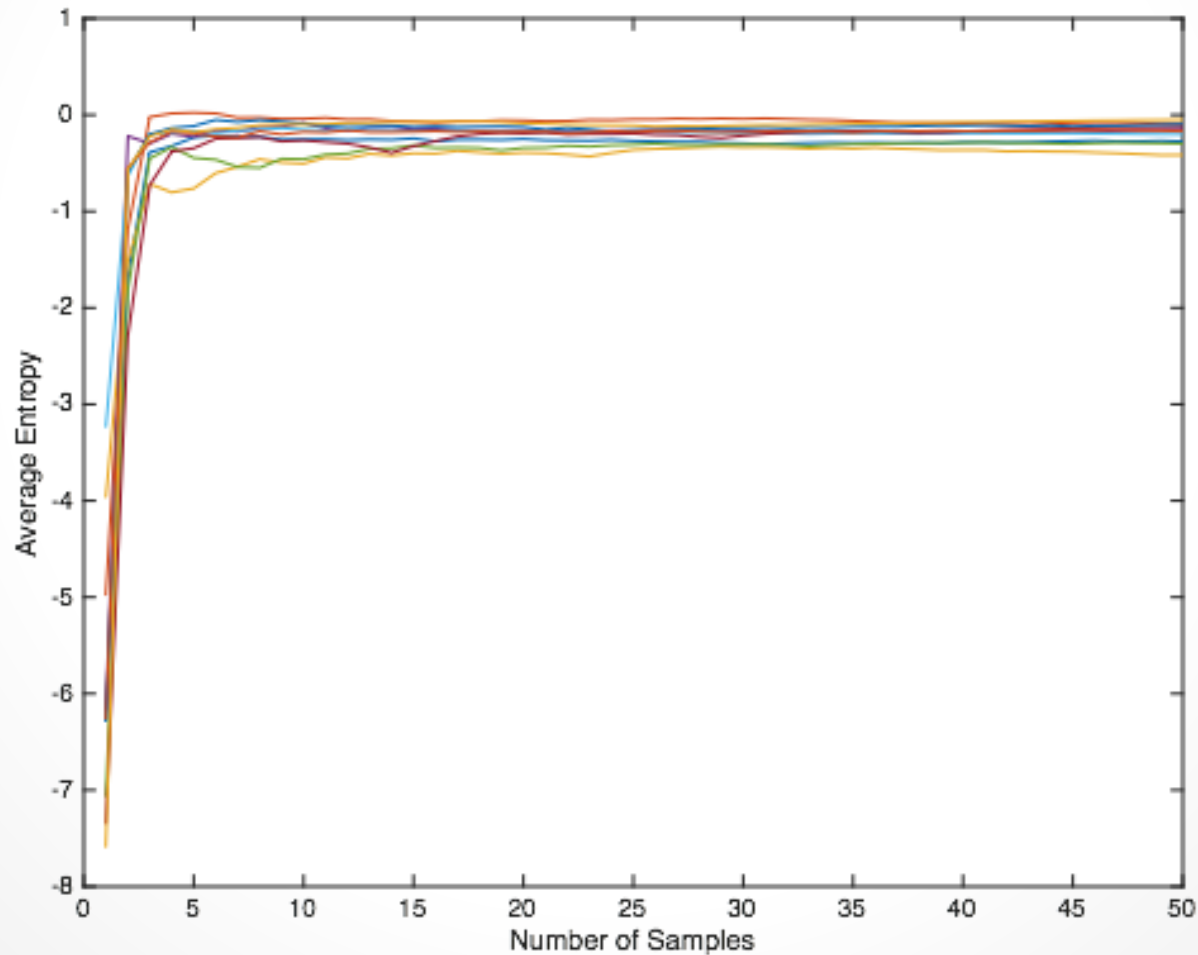
No. of Test Data = 10



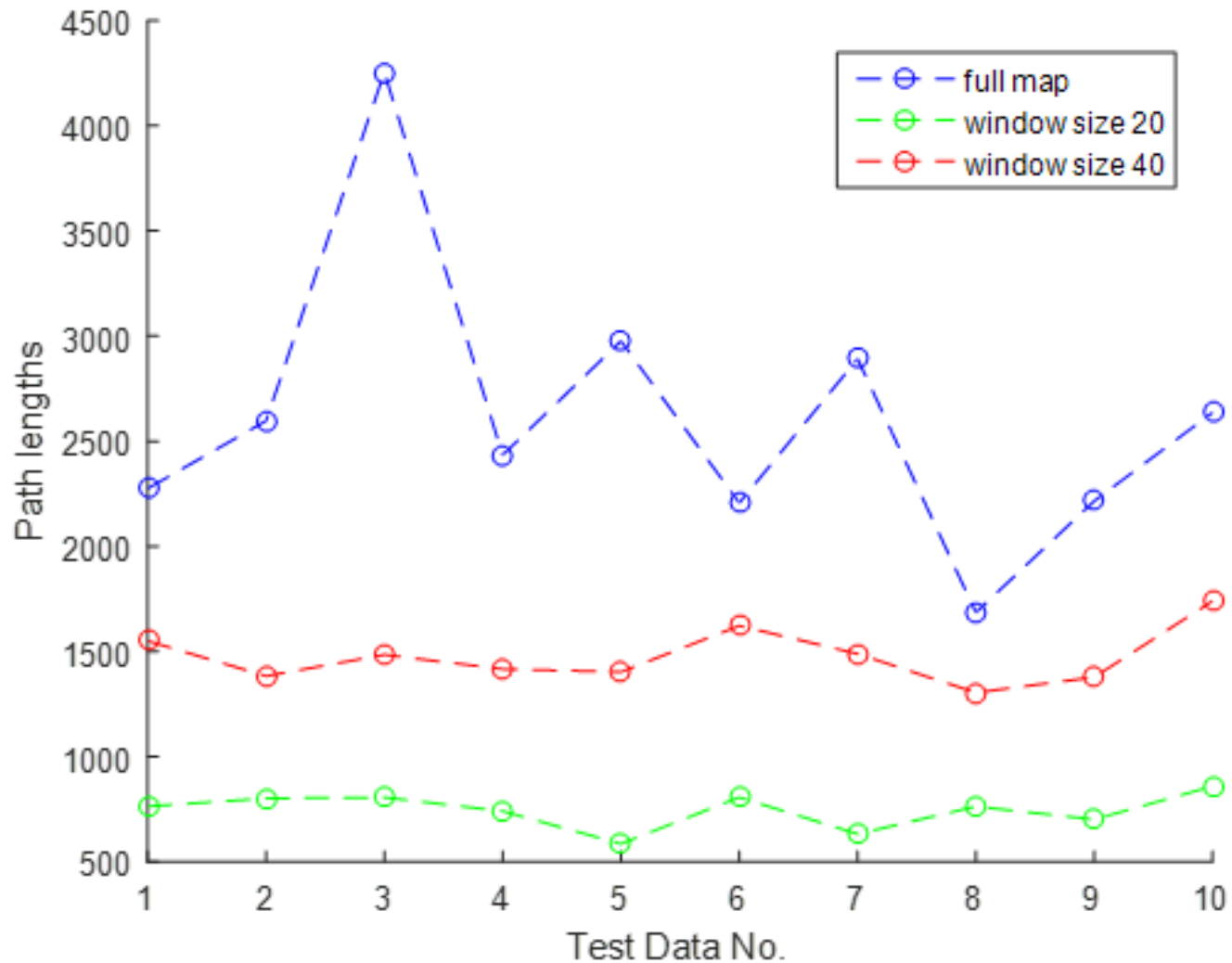
Greedy Approach - window

Window size +-40

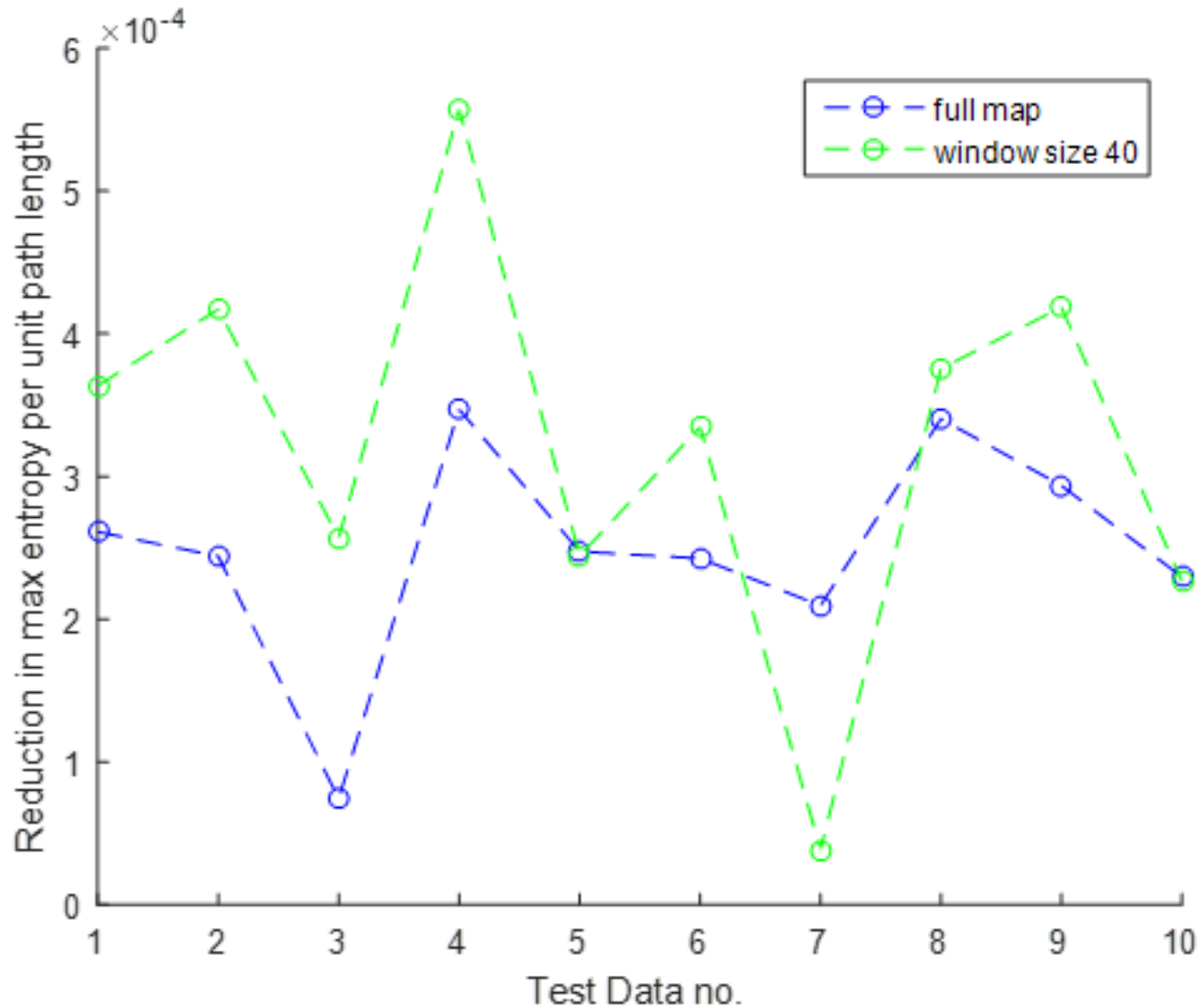
No. of Test Data = 10



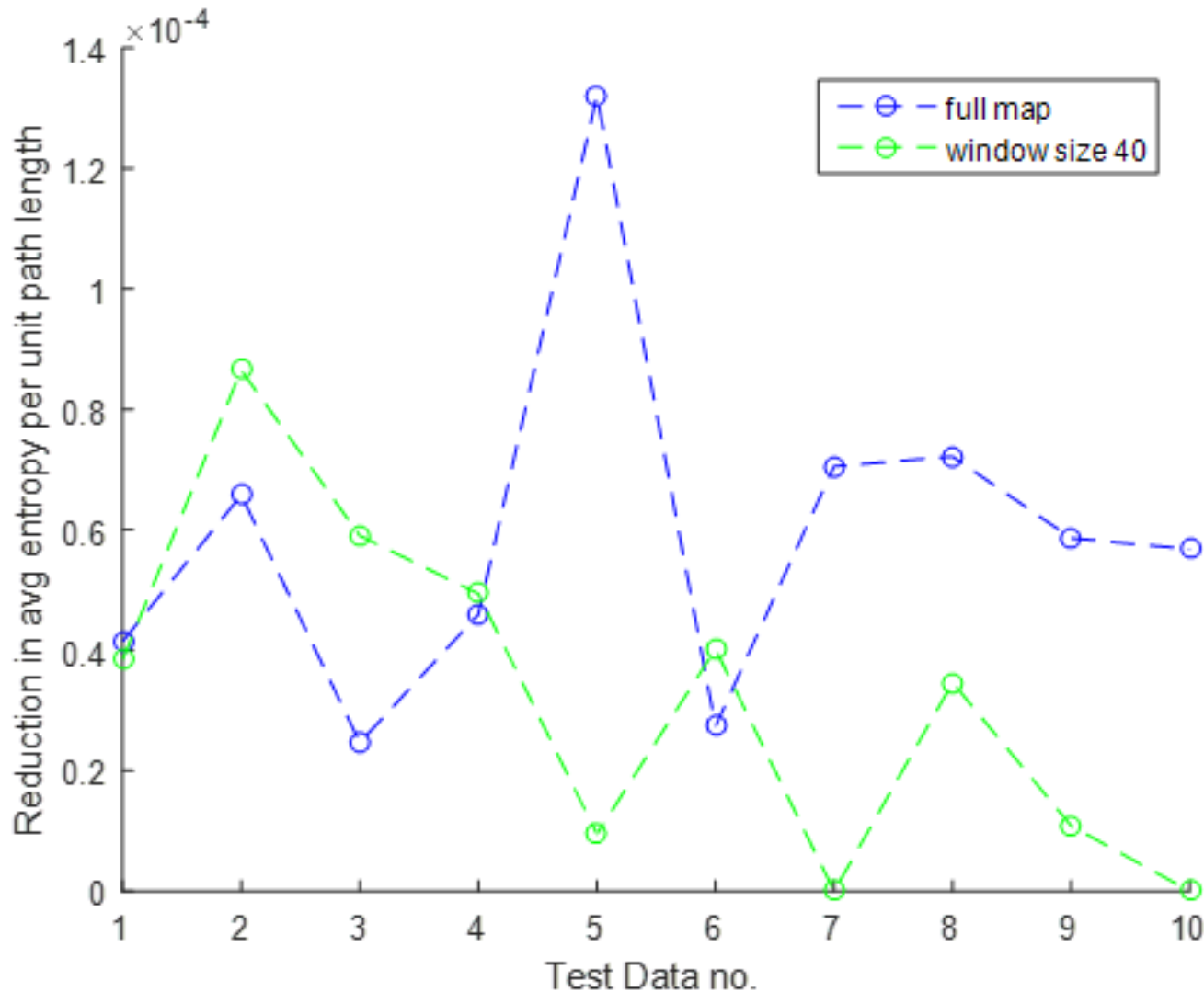
Paths lengths - Full vs window



Maximum Entropy reduction/path length - Full vs window



Average Entropy reduction/path length - Full vs window



Problem 1: Where to sample

A Mars rover is shown on a red, rocky planet surface. A bright green laser beam extends from the rover towards a large rock in the distance. The background shows a hazy, orange-red horizon under a clear sky.

Approach 2: Feature Space based Entropy

General Flow

Satellite Data in feature space

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graph TD; A[Satellite Data in feature space] --> B[Cluster]; B --> C[Probabilities and entropy calculation]; C --> D[Maximum entropy point sample]; D --> E[Replace sampled point with data and update];
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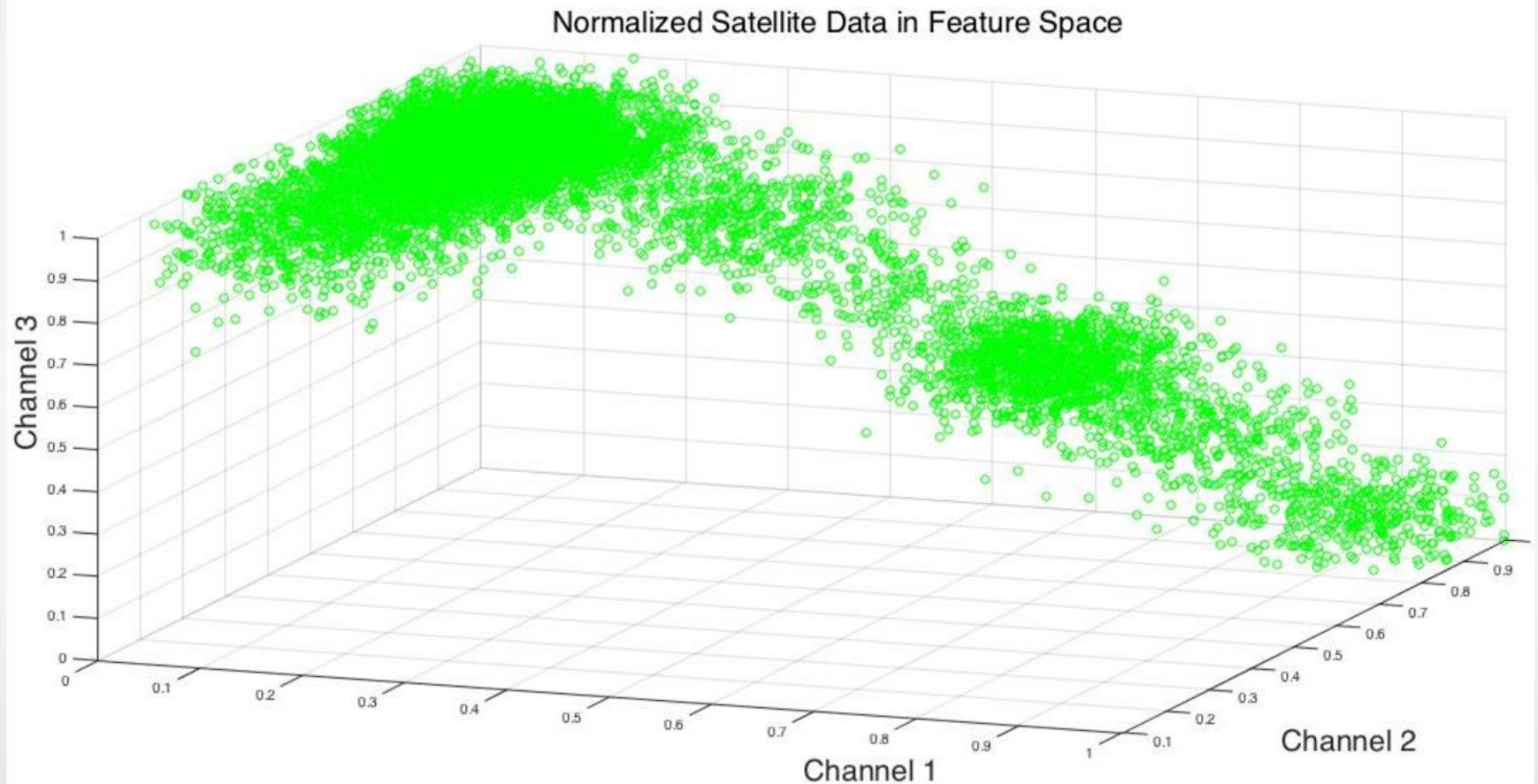
Cluster

Probabilities and entropy calculation

Maximum entropy point sample

Replace sampled point with data and update

Data in Feature Space

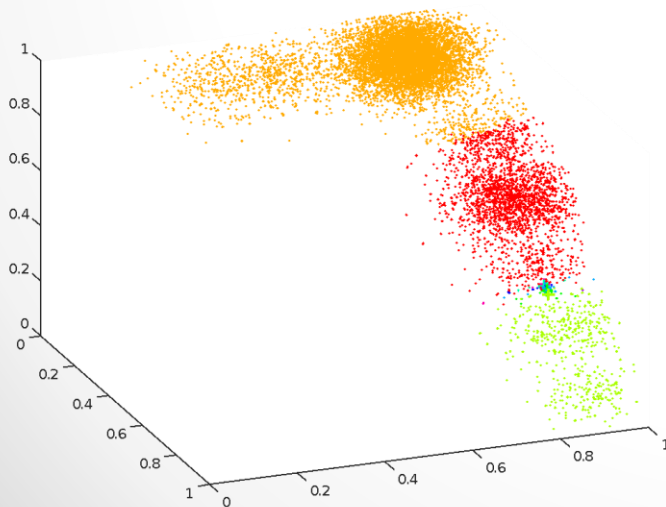


Clustering

- K-means
 - Parametric approach – assumes number of classes (not available)
- Mean-shift
 - Non-parametric approach – bandwidth keeps changing
 - Optimization parameter – people have done this...
 - might not capture the rare classes as they are sparse

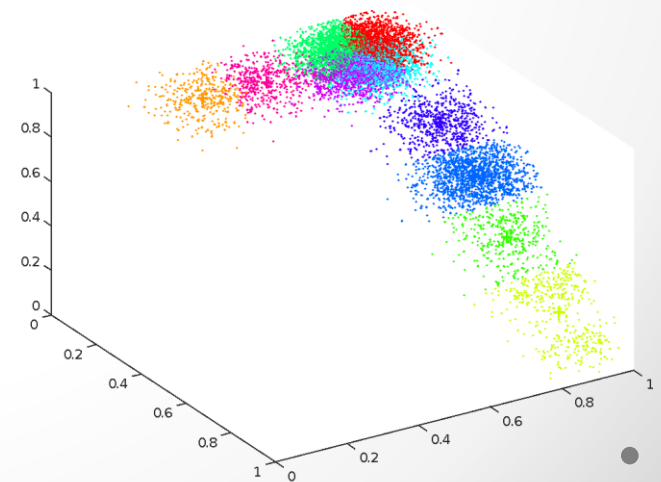
Meanshift (0.2)

ms_featurespaceTestData_1.mat



Kmeans

kmeans_featurespaceTestData_1.mat



Probability and Entropy

$$P_{ij} = \frac{1/d_{ij}}{\sum_{j=1}^J 1/d_{ij}}$$

i = feature point

j = cluster

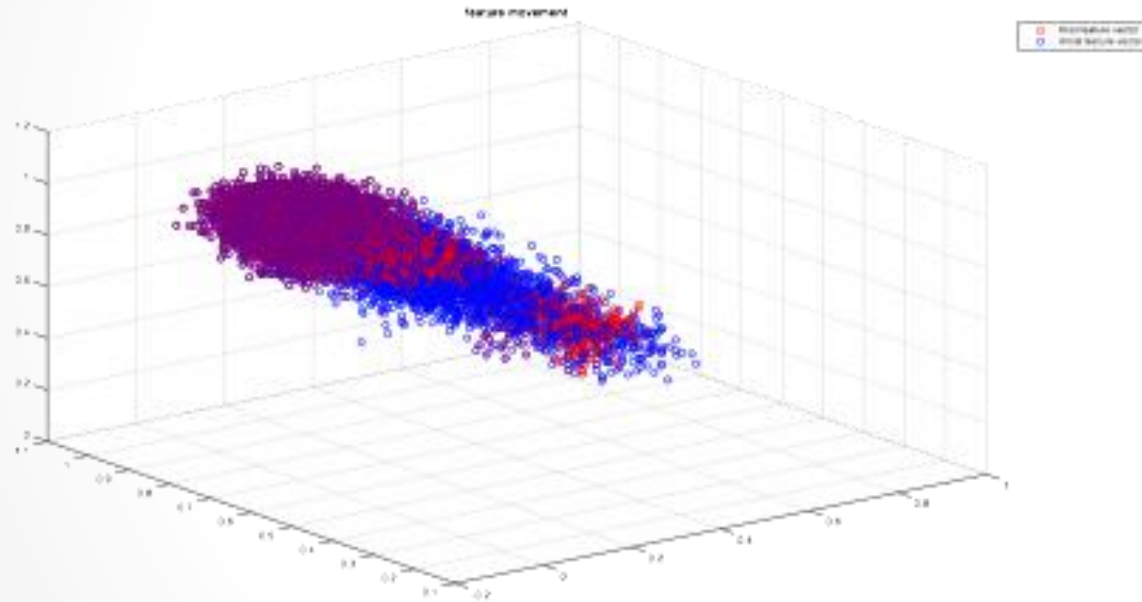
J = total number of clusters

$$H(i) = \sum_{j=1}^J P_{ij} \log_2 \left(\frac{1}{P_{ij}} \right)$$

Shannon's Entropy for each feature point

Units – bits (log base 2)

Re-sampling

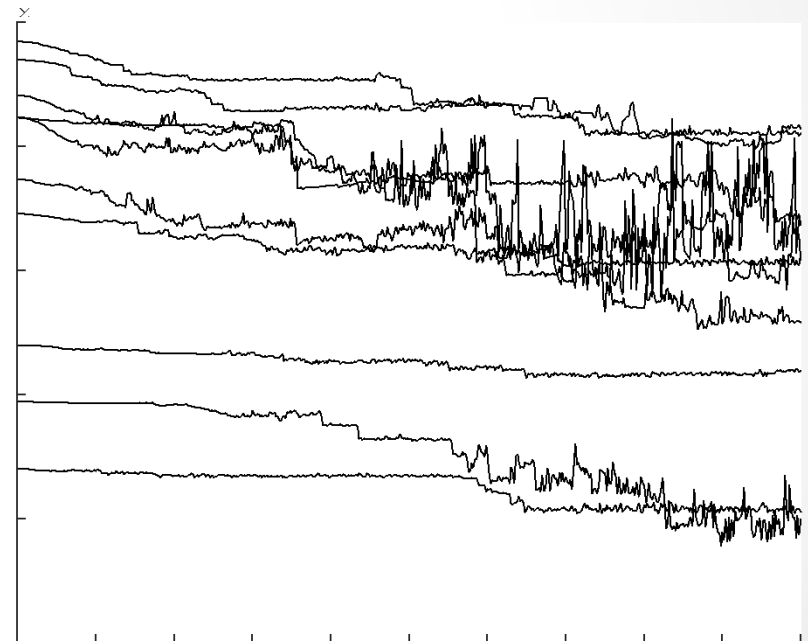


- Gaussian Kernel to move points around the sampled point

Results

2.96% decrease

1.25% decrease



Overall average entropy decrease in both methods..
Multiple parameters left to optimize!

Problem 2: Planning Path to Sampling Point

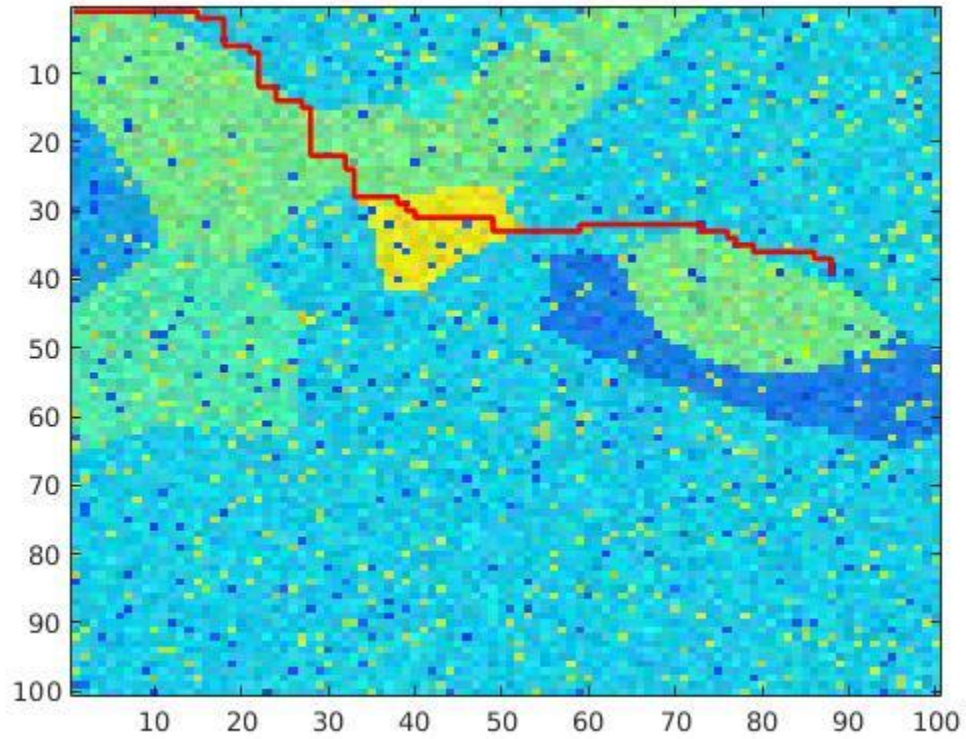
A photograph of a Mars rover on a red, rocky planet surface. A bright green laser beam originates from the rover's mast and extends horizontally across the middle of the frame towards a large rock on the right. The background shows a hazy, reddish horizon under a clear sky.

Approach 1: DP path length constraint
planning

DP approach

- Currently:
 - Budget based planning
 - Scientist guided
 - Heuristics to optimize
- Extreme case:
 - DP approach to find path with Maximum information gain, given a budget
 - Sets a reference for best solution for the budget
 - Cannot be used Dynamically -: Computation cost is very high

Paths Generated



Problem 2: Planning Path to Sampling Point

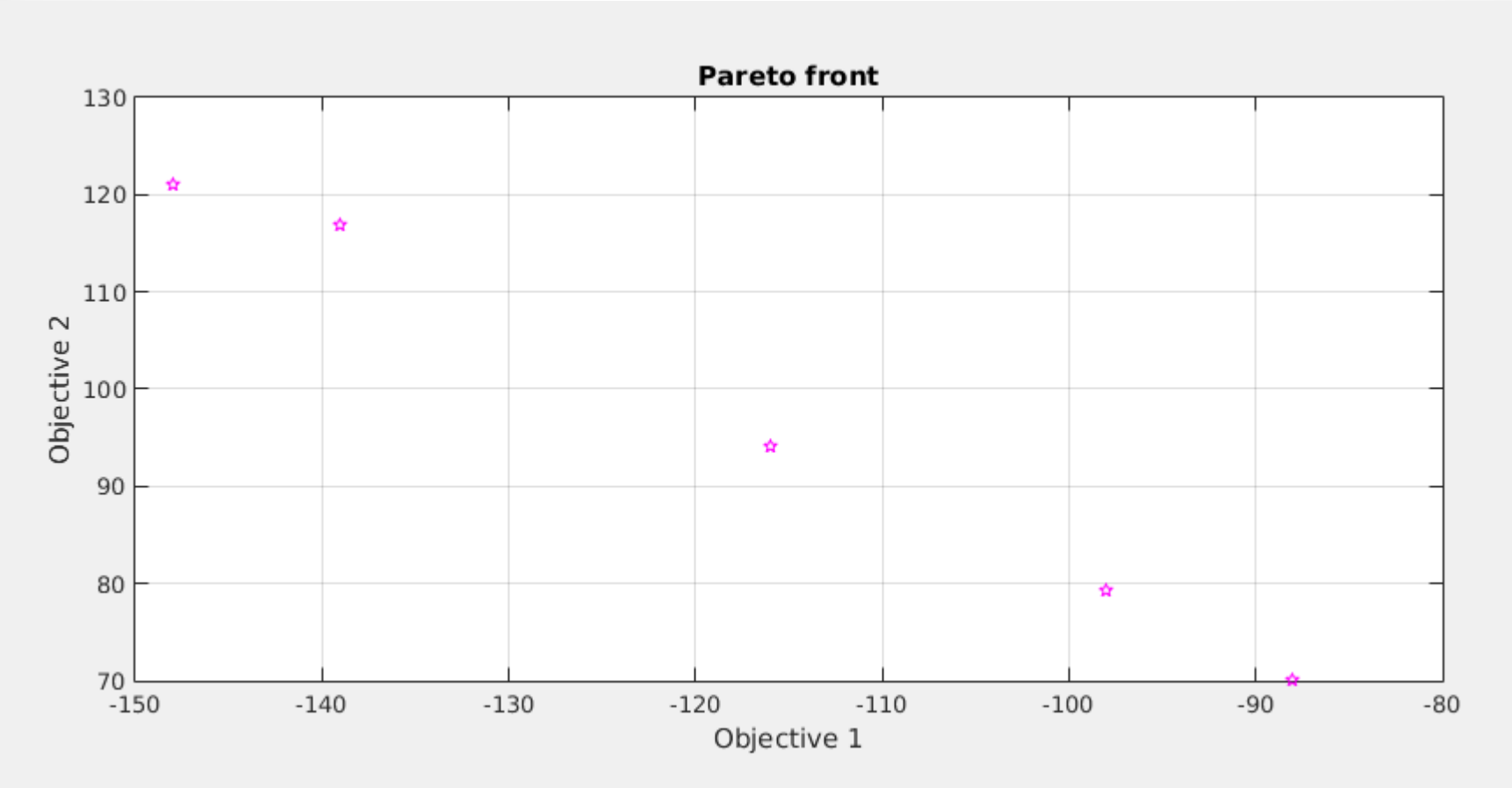
A photograph of a Mars rover on a red, rocky planet surface. A bright green laser beam originates from the rover's camera and points towards a large rock in the distance. The background shows a hazy, reddish horizon under a clear sky.

Approach 2: Multi-Heuristic A*

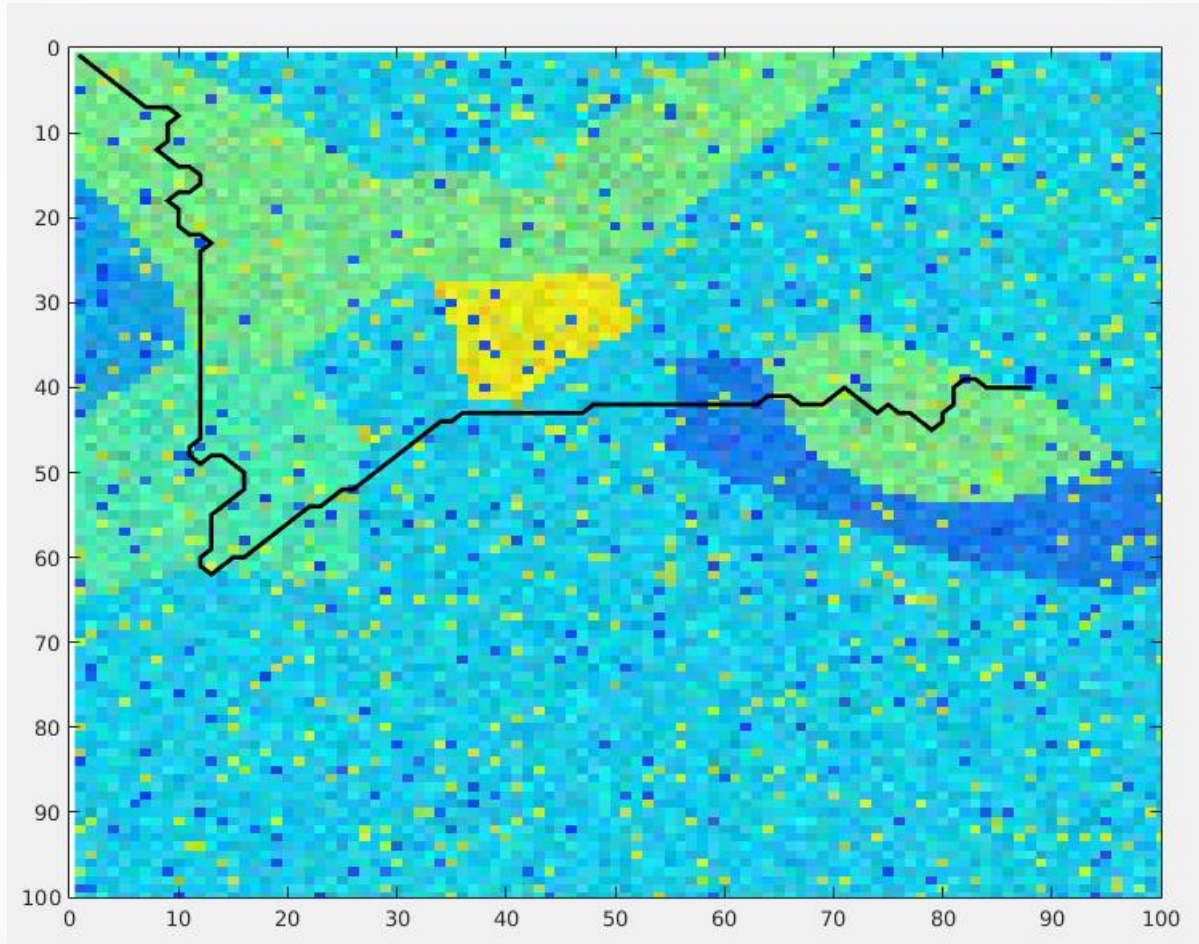
Multi-Heuristic A*

- Multiple Heuristics in Planning
 - Given a 'Global' Objective, Maximise Information Collected Along the Way
 - Distance as 'Anchor' heuristic
 - Information as an additional Heuristic
- Multi-Objective Optimisation
 - Maximise Information Gain
 - Minimize Path Length

Pareto Optimisation Curve

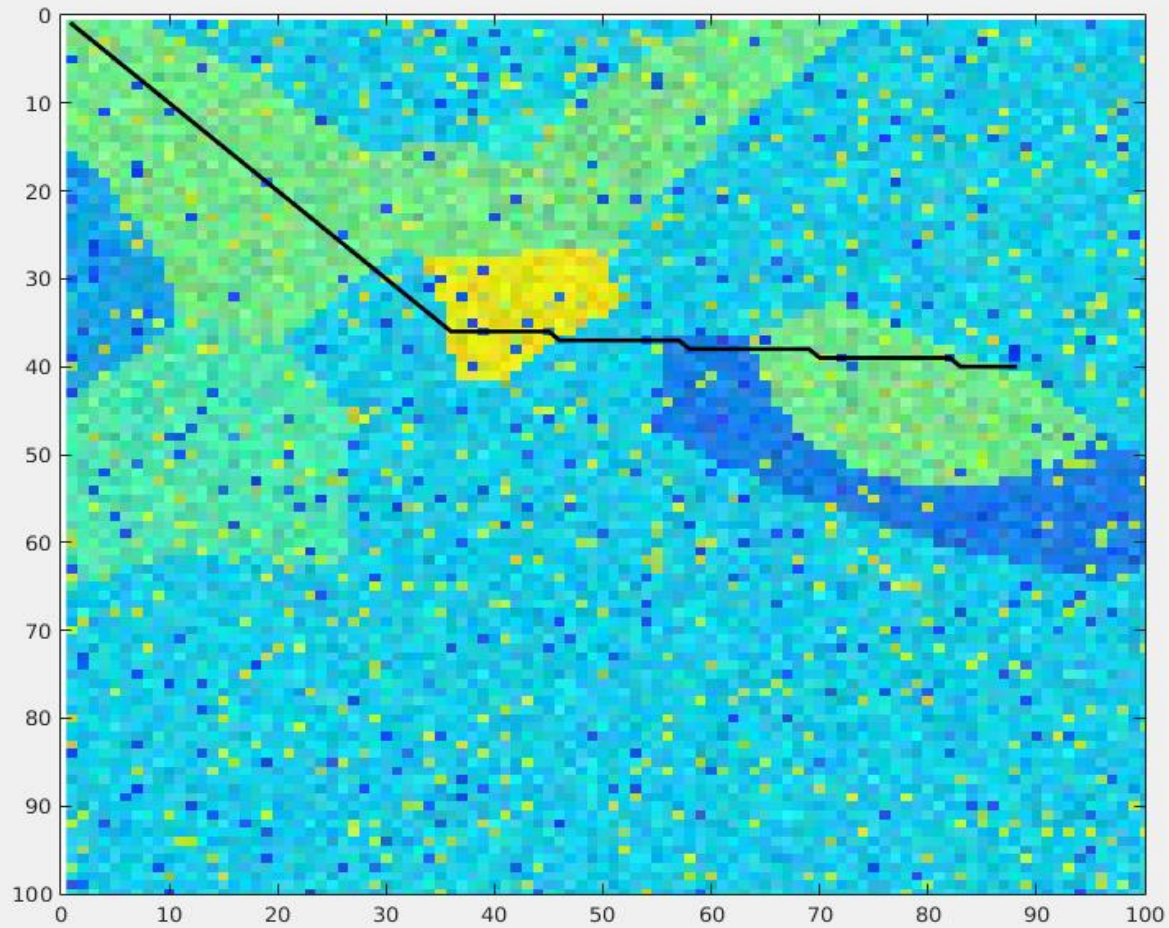


Paths Generated



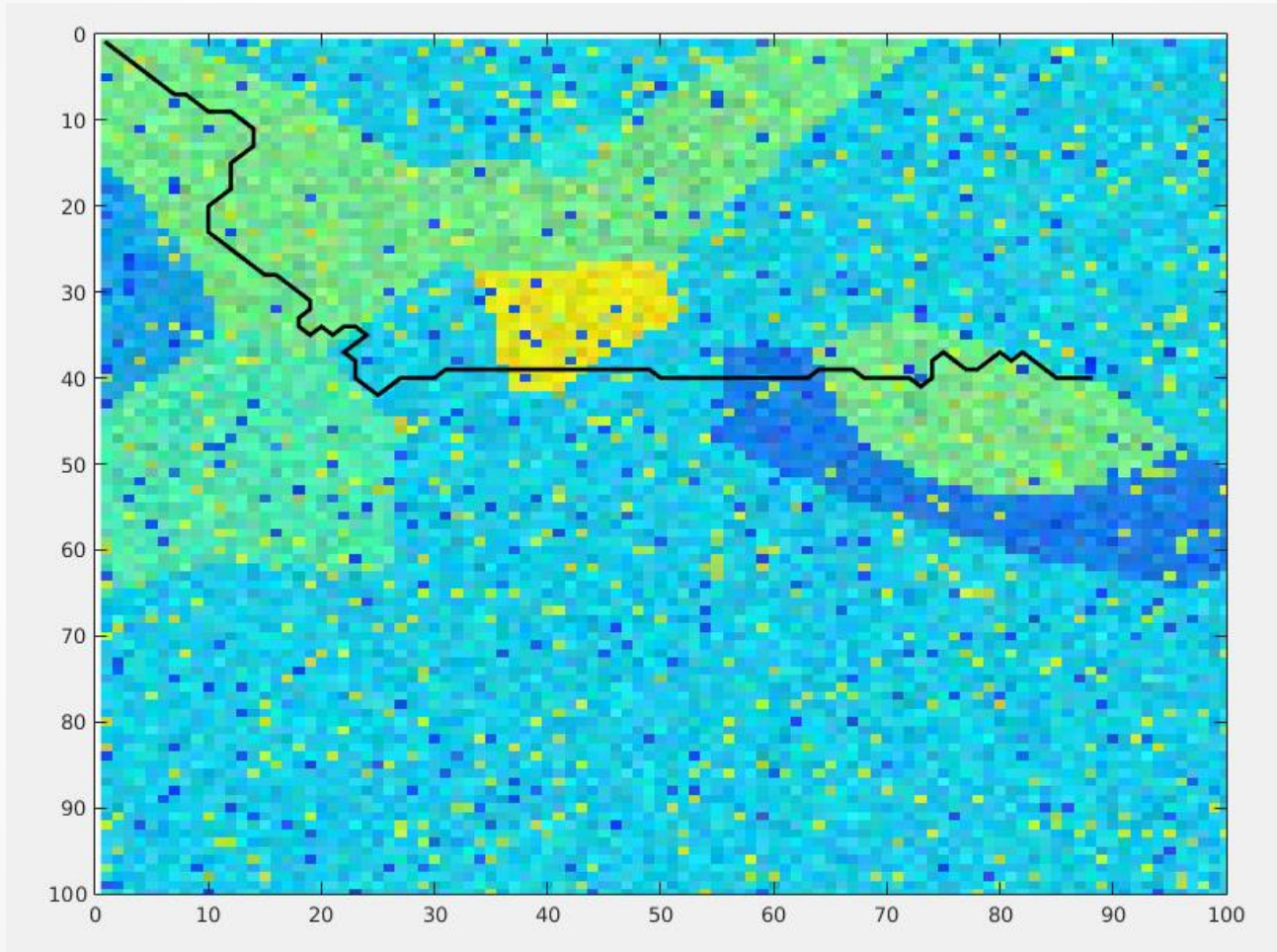
Weight of Information >> Weight of Distance

Paths Generated



Weight of Information \ll Weight of Distance

Paths Generated



Optimal Weights for Distance and Information

Statistical Comparison of Planning

Sno.	Technique	Percent Entropy Reduction	Entropy Reduction Per Unit Distance Travelled	Percent Entropy Reduction per Unit Distance Travelled	Runtime
1	Dynamic Programming	69.75%	211.66	0.5449%	5 hours
2	MHA*	46.875%	142.81	0.3982%	0.1s - 4s

Conclusion

- State of the art entropy calculation methods implemented
- Novel implementation of clustering based entropy done
- Planning in Euclidean space and Information space
- Multi Heuristic A*
- Dynamic Programming

Thank You!